

CHAPTER 1

RELATION & FUNCTIONS

ASSERTION & REASON QUESTIONS

SL.NO.	QUESTION
	Choose the correct option in the following questions of Assertion – Reason Questions. (a) Both A and R are correct; R is the correct explanation of A. (b) Both A and R are correct; R is not the correct explanation of A. (c) A is correct; R is incorrect. (d) R is correct; A is incorrect
1	Assertion (A) Let $A = \{a, b, c\}$, $B = \{4, 5, 6, 7\}$ and let $f = \{(a, 4), (c, 5), (b, 7)\}$ be a function from A to B. Then f is one-one. Reason (R) f is bijective function
2	Assertion (A) if $n(A) = 5$ and $n(B) = 4$ The number of relation from set A to B is 20 Reason (R) The number of subset of $A \times B$ is 2^{20}
3	Assertion(A) T is the set of triangle such that $\{(T_1, T_2) : T_1 \text{ is congruent to } T_2\}$. Then R is an equivalence relation. Reason(R) Any relation R is an equivalence relation, if it is reflexive, symmetric and transitive
4	Assertion(A) the function $f : \mathbb{R} \rightarrow \mathbb{R}$, given by $f(x) = 2x$, is one-one and onto. Reason(R) A function $f : X \rightarrow Y$ is said to be one-one and onto (or bijective), if f is both one-one and onto.
5	Assertion(A) The relation R on the set $\mathbb{N} \times \mathbb{N}$, defined by $(a, b) R (c, d) \Leftrightarrow a+d = b+c$ for all $(a, b), (c, d) \in \mathbb{N} \times \mathbb{N}$ is an equivalence relation. Reason (R) Any relation R is an equivalence relation, if it is reflexive, symmetric and transitive.
6	Assertion: If $f: \mathbb{R} \rightarrow \mathbb{R}$ defined by $f(x) = \sin x$ is a bijection. Reason: If f is both one- one and onto. It is bijection.
7	Assertion: Let L be the set of all lines in a plane and R be the relations in L defined as $R = \{(L_1, L_2) : L_1 \text{ is perpendicular to } L_2\}$. This relation is not equivalence relation. Reason: A relation is said to be equivalence relation, if it is reflexive, symmetric and

	transitive
8	<p>Assertion: Domain and range of the relation $R = \{(x, y) : x - 2y = 0\}$ defined on the set $A = \{1, 2, 3, 4\}$ are respectively $\{1, 2, 3, 4\}$ and $\{2, 4, 6, 8\}$</p> <p>Reason: Domain and Range of a relation R are respectively the sets $\{a : a \in A \text{ and } (a, b) \in R\}$ and $\{b : b \in A \text{ and } (a, b) \in R\}$</p>
9	<p>Assertion: The Greatest integer Function $f : R \rightarrow R$ is given by $(x) = [x]$ is not onto.</p> <p>Reason: A function $f : A \rightarrow B$ is said to be injective if $f(a) = f(b) \Rightarrow a = b$</p>
10	<p>Assertion: For two sets $A = R - \{3\}$ and $B = R - \{1\}$ defined a function $f : A \rightarrow B$ as $f(x) = \frac{x-2}{x-3}$ is bijective</p> <p>Reason: A function $f : A \rightarrow B$ is said to be surjective if for all $y \in B, \exists x \in A$ such that $f(x) = y$</p>
11	<p>Assertion (A): The relation R in the set $A = \{1, 2, 3, 4, 5, 6\}$ defined as $R = \{(a, b) : b \text{ is divisible by } a\}$ is not an equivalence relation.</p> <p>Reason (R) : The relation R will be an equivalence relation, if it is reflexive, symmetric and transitive.</p>
12	<p>Assertion (A): If $A = \{x \in Z : 0 \leq x \leq 12\}$ and R is the relation in A given by $R = \{(a, b) : a = b\}$, then the set of all elements related to 1 is $\{1, 2\}$.</p> <p>Reason (R) : If R_1 and R_2 are equivalence relation in a set A, then $R_1 \cap R_2$ is an equivalence relation.</p>
13	<p>Q3. Assertion (A): Let $f : R \rightarrow R$ be defined by $f(x) = x^2 + 1$, then the pre-image of 17 are ± 4.</p> <p>Reason (R) : A function $f : A \rightarrow B$ is called one-one function, if distinct elements of A have distinct images in B.</p>
14	<p>Assertion (A): Let a relation R defined from $A = \{1, 2, 5, 6\}$ to itself as $R = \{(1, 1), (1, 6), (6, 1)\}$, then R is symmetric relation.</p> <p>Reason (R) : A relation R in set A is said to be symmetric $(a, b) \in R \Rightarrow (b, a) \in R, a, b \in A$.</p>
15	<p>Assertion (A): The modulus function $f : R \rightarrow R$ be given by $f(x) = x$, is neither one-</p>

	<p>one nor onto</p> <p>Reason (R) : The signum function $f : R \rightarrow R$ given by $f(x) = \begin{cases} 1, & \text{if } x > 0 \\ 0 & \text{if } x = 0 \\ -1 & \text{if } x < 0 \end{cases}$ is bijective.</p>
16	<p>ASSERTION – The relation R given by $R = \{(1,3), (4,2), (2,4), (2,3), (3,1)\}$ on a set $A = \{1,2,3,4\}$ is symmetric.</p> <p>REASON – For symmetric relation $R = R^{-1}$</p>
17	<p>ASSERTION - let T be the set of all triangles in a plane with R being a relation in T given by $R = \{(T1, T2) : T1 \text{ is similar to } T2\}$. R is an equivalence relation.</p> <p>REASON- A reflexive symmetric and transitive relation is an equivalence relation.</p>
18	<p>ASSERTION- Let $f : R \rightarrow R$ defined as $f(x) = [x]$ where $[.]$ represents greatest integer function then f is not one- one.</p> <p>REASON- A function f is one -one if $f(\alpha) = f(\beta)$ implies $\alpha = \beta$</p>
19	<p>ASSERTION- Number of all on to functions from the set $\{1,2,3,4\}$ to itself is 24.</p> <p>REASON – On to functions from the set $\{1,2,3,\dots,n\}$ to itself is simply a permutation on n symbols namely $1,2,3,\dots,n$ is $n!$</p>
20	<p>ASSERTION- If $A = \{1,2\}$ then no of reflexive relations on A is 4 .</p> <p>REASON – No of reflexive relations define on a set of n elements is $2^{n(n-1)}$</p>
21	<p>Assertion (A) : If $n(A) = p$ and $n(B) = q$ then the number of relations from A to B is 2^{pq}.</p> <p>Reason (R) : A relation from A to B is a subset of $A \times B$.</p>
22	<p>Assertion(A): Domain and Range of a relation $R = \{(x,y) : x-2y=0\}$ defined on the set $A = \{1,2,3,4\}$ are respectively $\{1,2,3,4\}$ and $\{2,4,6,8\}$</p> <p>Reason: Domain and Range of a relation R are respectively the sets $\{a : a \in A \text{ and } (a,b) \in R\}$ and $\{b : b \in A \text{ and } (a,b) \in R\}$</p>
23	<p>Assertion (A): A relation $R = \{(1,1), (1,3), (1,5), (3,1), (3,3), (3,5)\}$ defined on the set $A = \{1,3,5\}$ is transitive.</p> <p>Reason(R): A relation R on the set A symmetric if $(a, b) \in R$ and $(a, c) \in R \Rightarrow (a,c) \in R$</p>
24	<p>Let R be the relation in the set of integers Z given by $R = \{(a, b) : 2 \text{ divides } a-b\}$</p> <p>Assertion (A): R is a reflexive relation.</p> <p>Reason (R): A relation is said to be reflexive if $xRx, \forall x \in Z$</p>
25	<p>Consider the function $f : R \rightarrow R$ defined as $f(x) = x/x^2 + 1$.</p> <p>Assertion (A): $f(x)$ is not one-one.</p> <p>Reason (R): $f(x)$ is not onto.</p>
26	<p>Assertion (A): The relation R on the set $N \times N$, defined by $(a, b) R (c, d) \Leftrightarrow a+d = b+c$ for all $(a, b), (c, d) \in N \times N$ is an equivalence relation.</p>

	Reason (R): Any relation R is an equivalence, if it is reflexive, symmetric and transitive
27	Assertion (A): $f(x) = 1 + x^2$ is a one to one function from $\mathbb{R}^+ \rightarrow \mathbb{R}$, Reason (R): Every strictly monotonic function is a one to one function.
28	Let W be the set of words in the English dictionary. A relation R is defined on W as $R = \{(x, y) \in W \times W \text{ such that } x \text{ and } y \text{ have at least one letter in common}\}$ Assertion (A): R is reflexive. Reason (R): R is symmetric.
29	Consider the set $A = \{1, 3, 5\}$. Assertion (A): The number of reflexive relations on set A is 2^9 . Reason (R): A relation is said to be reflexive if $xRx, \forall x \in A$.
30	Consider the function $f : \mathbb{R} \rightarrow \mathbb{R}$ defined as $f(x) = x^3$ Assertion (A): $f(x)$ is one – one function. Reason (R): $f(x)$ is one – one function if co-domain = range.
31	Assertion (A) If $n(A) = p$ and $n(B) = q$ then the number of relations from A to B is 2^{pq} . Reason(R) A relation from A to B is a subset of $A \times B$.
32	Assertion (A) If $n(A) = m$, then the number of reflexive relations on A is m Reason(R) A relation R on the set A is reflexive if $(a, a) \in A$
33	Assertion (A) A relation $R = \{(1,1), (1,2), (2,2), (2,3), (3,3)\}$ defined on the set $A = \{1,2,3\}$ is reflexive. Reason(R) A relation R on the set A is reflexive if $(a,a) \in R$, for all a belongs to A
34	Assertion (A) : $A = \{1,2,3\}, B = \{4,5,6,7\}, f = \{(1,4), (2,5), (3,6)\}$ is a function from A to B. Then f is one-one Reason(R) : A function f is one –one if distinct elements of A have distinct images in B.
35	Assertion (A): $n(A) = 5, n(B) = 5$ and $f : A \rightarrow B$ is one-one then f is bijection

	Reason(R): If $n(A)=n(B)$ then every one-one function from A to B is onto
36	Assertion: A relation $R = \{1,1\}$ in the set $A = \{1,2,3\}$ is a reflexive relation. Reasoning: To be reflexive $(a, a) \in R, \forall a \in A$
37	Assertion: A relation $R = \{1,2\}$ in the set $A = \{1,2,3\}$ is a transitive relation. Reasoning: To be transitive $(a, b) \in R$ and $(b, c) \in R \Rightarrow (a, c) \in R$
38	Assertion: A relation $R = \{(1,2), (2,1), (1,1), (2,2), (3,3)\}$ in the set $A = \{1,2,3\}$ is an equivalence relation. Reasoning: To be symmetric $(a, b) \in R \Rightarrow (b, a) \in R$
39	Assertion: A function $f: \mathbb{R} \rightarrow \mathbb{R}$ defined by $f(x) = x $ is not onto. Reasoning: Range of $f = \mathbb{R}^+$.
40	Assertion: A function $f: \mathbb{R} \rightarrow \mathbb{R}$ defined by $f(x) = e^x$ is not onto. Reasoning: Range of $f \neq \mathbb{R}$ (Codomain).
41	Assertion: Every equivalence relation is reflexive also. Reason: Every reflexive relation is equivalence relation.
42	Assertion: A relation from set A to B is a subset of $A \times B$. Reason: \emptyset is subset of every set.
43	Assertion: A one – one function $f: \{1,2,3,4,5\} \rightarrow \{1,2,3,4,5\}$ is onto. Reason: A one – one function from an arbitrary set X to itself is always onto.
44	Assertion: A function $f: \mathbb{N} \rightarrow \mathbb{N}$ given by $f(x) = x^2$ is onto. Reason: A function $f: X \rightarrow Y$ is said to be onto if every element of Y is image of some element of X under f.
45	Assertion: The relation R in the set $\{x \in \mathbb{Z} : -1 < x < 13\}$ defined as $R = \{(a,b) : a - b \text{ is an integer}\}$ is symmetric. Reason: A relation R in a set A is called reflexive if every element of set A is related to itself.
46	Let R be the relation in the set of integers \mathbb{Z} given by $R = \{(a,b) : 2 \text{ divides } a-b\}$ A: R is a reflexive relation R: A relation is said to be reflexive if $xRx, x \in \mathbb{Z}$
47	If $A = \{1,2,3\}$, $B = \{4,5,6\}$ and $f = \{(1,4), (2,5), (3,6)\}$ is a function from A to B A: $f(x)$ is one-one function

	R: $f(x)$ is onto function
48	Consider a set $A=\{a,b,c\}$. A: the no of reflexive relations on the set A is 2^9 R: the relation is said to be reflexive if $xRx, x \forall A$
49	Let a function $f: \mathbb{R} \rightarrow \mathbb{R}$ defined by $f(x)=x^2$ A: f is many-one R: $f(-x)=f(x)=x^2, x \forall \mathbb{R}$
50	Let W be the set of words in English dictionary. A relation R is defined on W as $R = \{(x, y) \in W \times W \text{ such that } x \text{ and } y \text{ have at least one letter in common}\}$ Assertion: R is reflexive. Reason: R is symmetric.
51	Assertion: The function $f(x)$ given by $f(x) = \sin^{-1} \left[\log \left(x + \sqrt{x^2 + 1} \right) \right]$ is an odd function. Reason: The composition of two odd function is an odd function. (a) 1 (b) 2 (c) 3 (d) 4
52	Assertion: Every function can be uniquely expressed as the sum of an even function and an odd function. Reason: The set of values of parameter a for which the function $f(x)$ defined as $f(x) = \tan(\sin x) + \frac{x^2}{a}$ on the set $[-3,3]$ is an odd function is, $[9, \infty)$ (a) 1 (b) 2 (c) 3 (d) 4
53	Assertion: If $ad - bc \neq 0$, then $f(x) = \frac{ax+b}{cx+d}$ cannot attain the value $\left\{ \frac{a}{c} \right\}$ Reason: The domain of the function $g(x) = \frac{b-dx}{cx-a}$ is $R - \left\{ \frac{a}{c} \right\}$ (a) 1 (b) 2 (c) 3 (d) 4
54	Assertion: $f(x) = x-2 + x-3 + x-5 $ is an odd function for all values of x between 3 and 5. Reason: $f(-x) = -f(x)$ for all odd functions. a) 1 (b) 2 (c) 3 (d) 4
55	Assertion: The domain of definition of the function $f(x) = e^{2x} + \cos^{-1} \left(\frac{x}{2} - 1 \right)$ is $(0,1) \cup (1,2) \cup (2,3) \cup (3,4)$ Reason: The domain of $\cos^{-1} \left(\frac{x}{2} - 1 \right)$ is $(0,4)$ a) 1 (b) 2 (c) 3 (d) 4
56	A : If the set A contains 5 elements and the set B contains 6 elements , then the number

	<p>of one-one and onto mappings from A to B is 0</p> <p>R: If A and B are two non empty finite sets containing m elements and n elements respectively , then the number of one-one and onto mappings from A to B is $n!$ if $m = n$ and 0 if $m \neq n$</p>
57	<p>A :The function $f(x) = x$ is not one -one.</p> <p>R :The function $f(x) = x$ is onto.</p>
58	<p>A: A relation $R = \{ (1,1), (1,2), (2,2), (2,3), (3,3) \}$ defined on the set $A = \{ 1,2,3 \}$ is reflexive.</p> <p>R: A relation R on the set A is reflexive if $(a,a) \in R, \forall a \in A$</p>
59	<p>A:Let $f : X \rightarrow Y$ be a function. Define a relation R on X given by $R = \{ (a,b) : f(a) = f(b) \}$. Then R is equivalence relation.</p> <p>R: R is not symmetric.</p>
60	<p>If $f : R \rightarrow R$ is an injective function such that range of $f = \{a\}$, then the number of elements in A is 1.</p> <p>R: f is one – one function so different element of A has different images.</p>

ANSWER KEY

1	C	16	D	31	A	46	A
2	D	17	A	32	D	47	B
3	A	18	A	33	A	48	A
4	A	19	C	34	A	49	A
5	A	20	A	35	A	50	B
6	D	21	A	36	D	51	A
7	A	22	D	37	A	52	B
8	D	23	C	38	B	53	A

9	B	24	A	39	C	54	B
10	B	25	B	40	A	55	C
11	A	26	A	41	C	56	A
12	D	27	A	42	B	57	A
13	B	28	B	43	C	58	D
14	A	29	D	44	D	59	C
15	C	30	C	45	B	60	A

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